

Here are some remarks on what you should have noticed from the first set of problems.

1. The association  $E \mapsto V(E)$  from subsets of a ring  $A$  to the set of prime ideals containing  $E$  in the set  $X = \text{Spec}(A)$  is inclusion reversing. If  $E$  is contained in  $F$ , then  $V(E)$  contains  $V(F)$ .
2. The above association only 'remembers' radicals of ideals, in the sense that if two ideals  $I$  and  $J$  have the same radical then  $V(I) = V(J)$ ; in geometry this translates to the notion of being reduced.
3. At the level of basic open sets in  $X = \text{Spec } A$ , the ring associated to an open set  $U_f$  is the ring  $A_f$ , which is the ring  $A$  localized at the multiplicative set  $\{1, f, f^2, \dots\}$ . Thus the set  $X = \text{Spec } A$  is actually what is called a ringed space.